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Memory Effects in Dynamical Many-Body Systems: The Isomnesic (Constant-Memory) Approximation

bу

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Memory Effects in Dynamical Many-Body Systems: The Isomnesic (Constant-Memory) Approximation

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Abstract

Exact numerical solutions of a generalized master equation for a system involving a temporally localizable memory kernel and a constant one are presented. Comparison with an isomnesic (constant-memory) approximation, with the memory kernel reduced to the sum of a local and a constant term, gives excellent agreement. A Markovian version of the problem is also described and found to be inherently ambiguous, devoid of significant physical features seen in the transient regions, but leading to the same steady-state as the isomnesic approximation.

I. Introduction

The dynamics of a system of many interacting particles is often treated by partitioning the system into two or more subsystems, one of which, \mathbf{S} , comprises the degree(s) of freedom of primary interest, while the others, \mathbf{R}_1 , \mathbf{R}_2 , ..., are reservoirs to which \mathbf{S} is coupled. No observations are made on the reservoirs, and the corresponding degrees of freedom are projected out of the equations of motion. A quantum mechanical generalized master equation (GME) results, and invokation of the Born and random-phase approximations generates a set of coupled Volterra-type integrodifferential equations (VTE)

$$P_{S}(t) = \sum_{S' \neq S} \int_{0}^{t} dt' [K_{SS}(t-t')P_{S'}(t') - K_{SS'}(t-t') P_{S}(t')], \qquad (1)$$

where $P_S(t)$ is a diagonal matrix element of the projected density operator in the subspace \mathbf{S} , and represents the probability of finding \mathbf{S} in an eigenstate $|S\rangle$ of the zero-order sub-Hamiltonian $\mathbf{J}_{\mathbf{C}}$:

$$\mathcal{J}(\mathbf{c}_{\mathbf{S}}|\mathbf{S}) = \mathbf{c}_{\mathbf{S}}|\mathbf{S} . \tag{2}$$

The kernel functions $K_{SS'}(t-t')$ include temporal correlations between dynamical variables of the reservoirs.² The resulting dependence of the state of \mathbf{S} at any time t upon all previous times $t' \leq t$, the memory effect, is manifested in the convolution form of $K_{SS'}(t-t')$, the memory kernels.³ For most real physical systems, the form of $K_{SS'}$ precludes an analytic closed-form solution, and often even step-by-step numerical integration.⁴ When numerical solutions using alternative techniques such as the method of successive approximations⁵ are possible, one is limited to small times. For example, for kernels with some form of periodicity, a fairly common situation, these times are of the order of

a few periods, which seldom correspond to macroscopic measurement times. The solutions are therefore of little use in suggesting or elucidating physical mechanisms.

The need for numerical solutions has, in the past, been circumvented by making the Markovian approximation (MA), 6,7 namely that the system is amnesic (has negligible memory). Thus the convolution-type kernels are assumed to be extremeley localized temporally,

$$K_{SS}, (t-t') = W_{SS}, \delta(t-t'), \qquad (3)$$

which is tantamount to assuming that the probability functions are very slowly varying during the (small) period of time in which K_{SS} , (t) changes substantially. This approximation is difficult to justify in general, and is in fact not justified if a locally correct solution is sought. This is because $P_S(t)$ must reflect the nature of K_{SS} , (t) itself, and if the latter varies substantially in any time range, so must $P_S(t)$, at least locally in time. What makes the MA useful is its avowed ability to provide the rough behavior of $P_S(t)$ over long time periods. Thus on a coarse-grained time scale, the MA is expected to provide results roughly resembling the exact results.

Not all physical systems admit of the representation of K_{SS} , (t-t') shown in Eq. (3), an important example being a system resonantly pumped by a continuous-wave laser and coupled to another reservoir. For this important class of physical systems the kernels can, under favorable conditions to be described later, be written as sums of terms such as Eq. (3) and additional constants independent of time. The resulting equations of motion are very different from those obtained using Eq. (3). The differences are quantified and highlighted in this work, and it is shown that the results of the exactly-solvable equations with kernels including the constants provide an excellent

representation of the solutions. The MA, on the other hand, is shown to lead to probability profiles in gross disagreement with the exact results, especially for the short time scale.

The format of this paper is as follows. In Section II the basic theory is summarized, and the results of calculations are presented in Section III.

Conclusions are given in Section IV.

II. The Isomnesic (Constant-Memory) Approximation

A system of great current interest that lends itself ideally as a vehicle for illustrating the various approximations for the memory kernel is an adatom adsorbed on a solid surface, vibrationally excited by an infrared continuous-wave laser, and coupled to phonon modes of the solid. $^{2,7-9}$ The system Sis the adbond, viz, the bond resulting from the interaction of the adatom with the phonon-averaged motion of the lattice atoms; 10 the phonons and the laser are two independent, noninteracting reservoirs \mathbf{R}_1 and \mathbf{R}_2 . Quantum theoretical treatments of this class of systems lead quite generally to a GME and a corresponding VTE, Eq. (1), with $\mathbf{P}_{\mathbf{S}}(\mathbf{t})$ representing the probability of finding the adbond in the eigenstate $|\mathbf{S}\rangle$ of the zero-order adbond Hamiltonian $\mathbf{R}_{\mathbf{S}}$. The kernels $\mathbf{K}_{\mathbf{SS}}$, (t-t') incorporate the influence of the phonons and the laser. We have partitioned the total Hamiltonian of the system in such a way that the perturbations which generate the kernels are traceless in their individual reservoir subspaces, 2,10 As a direct consequence, the total kernels separate into individual subspace kernels,

$$K_{SS}(t) = K_{SS}(p)(t) + K_{SS}(r)(t),$$
 (4)

where $K_{SS}^{(p)}(t)$ is due to the phonon field alone and $K_{SS}^{(r)}(t)$ is due to the laser radiation field alone. Using a one-dimensional model for the solid,

we have obtained the kernels in closed form and solved them numerically by an iterative technique⁵ for times of the order of a few "periods" of K_{SS} ,(t). These periods are dictated by the characteristic frequencies of the phonons and the adbond (i.e., the Debye frequency ω_D and the transition frequencies ω_{SS} , for bound states of the Hamiltonian 36, and the laser frequency ω_L all of which are $-10^{12}-10^{14}$ Hz (1-100 THz). The periods are therefore very small, being $-10^{-12}-10^{-14}$ s (1-.01 ps); consequently, the solutions of the VTE can be obtained numerically for times no larger than about 10 ps, which is certainly insufficient for the description of a physical or chemical process. In order to obtain solutions for longer times, an analytic solution must be sought.

We begin with the assertion that the physically important situation is one where the laser frequency and the Debye frequency equal different transition frequencies ω_{SS} , of the adbond. For this case $K_{SS}^{(r)}(t)$ becomes a constant $k_{SS}^{(r)}(t)$ from the term with $|\omega_{SS}| = \omega_L$ plus oscillating terms which we ignore in the sense of the rotating-wave approximation. The phonon term, $K_{SS}^{(p)}(t)$, has a complicated behavior typified by $K_{O1}^{(p)}(t)$ in Fig. 1, but we note that it has appreciable magnitude for times ~ 2 ps, and almost vanishes subsequently. If the mesh size of our theoretical experiment is no less than 2 ps, we can treat $K_{SS}^{(p)}(t)$ as a delta function, so that, from Eq. (4),

$$K_{gg}(t) = \Omega_{gg}(t) + k_{gg}(t) + k_{gg}(t)$$
 (5)

where

$$\Omega_{SS}^{\prime} = \int_{0}^{\infty} dt \, K_{SS}^{(P)}(t) . \qquad (6)$$

In Eq. (5), the first term, originating from the coupling of the adbond to the phonons, is the amnesic or Markovian term, and would lead, in the absence of the laser term, to the elimination of all memory effects. The second term, due to

the resonant laser coupling, is the isomnesic non-Markovian term, and represents a constant memory effect all the way back to t=0.

The subsequent treatment is simplified by defining "diagonal" elements $\Omega_{\mbox{SS}}$ and $k_{\mbox{SS}}$, viz.

$$\Omega_{SS} = -\sum_{S' \neq S} \Omega_{SS'}, \qquad (7)$$

$$k_{SS} = \sum_{S' \neq S} k_{S'S}$$
 (8)

and the notation

$$\hat{\Omega} = \{\Omega_{SS}, \}, \qquad (9a)$$

$$\underline{k} = \{k_{SS}, \}$$
, (9b)

$$K(t) = \{K_{SS}, (t)\},$$
 (9c)

$$\underline{\mathbf{W}} = \{\mathbf{W}_{SS}, \}, \tag{9d}$$

$$\underline{\Delta} = \{\delta_{SS}, \}, \qquad (9e)$$

$$\underline{P}(t) = \{P_{S}(t)\}. \tag{9f}$$

The exact VTE may be written as

$$\underbrace{P}(t) = \begin{cases} t \\ dt' \underline{K}(t-t') \cdot \underline{P}(t'); \end{cases}$$
 (10)

in the isomnesic approximation (IA) it becomes

$$\frac{P}{P}(t) = \underline{k} \cdot \begin{cases} t \\ dt' \underline{P}(t') + \underline{\Omega} \cdot \underline{P}(t) \end{cases}$$
(11)

Formally this can be solved without any further approximations. Differentiating both sides of Eq. (11), we get the second-order differential equation

$$\underline{\underline{P}}(t) = \underline{k} \cdot \underline{\underline{P}}(t) + \underline{\Omega} \cdot \underline{\underline{P}}(t) , \qquad (12)$$

whose Laplace transform,

$$\underline{M}(s) \cdot \underline{P}(s) = \underline{T}(s) , \qquad (13)$$

where

$$\underline{M}(s) = \underline{K} + s\underline{\Omega} - s^2\underline{\Delta} , \qquad (14)$$

$$\underline{\mathbf{T}}(\mathbf{s}) = -\mathbf{s}\underline{\mathbf{P}}(\mathbf{0}) , \qquad (15)$$

and $\mathcal{L}(s)$ is the Laplace transform of P(t), is easily inverted using the Heaviside expansion theorem.

While this effectively eliminates the non-Markovian bottleneck without recourse to Eq. (3), it is instructive to generate solutions of a Markovian version of this class of problems. To do this, we have to make provisions for localizing $K_{SS}^{(r)}$, in time. This brings to the fore the pervasive issue of time scales in dynamical many-body systems, our specific question being the relative degree of localization ascribable to $K_{SS}^{(p)}$ and $K_{SS}^{(r)}$. If the laser radiation is localized as a pulse, it can still extend over a period of time much longer than the extent of $K_{SS}^{(p)}(t)$. In other words, the delta function representing $K_{SS}^{(p)}(t)$ may be quite different from the delta function representing $K_{SS}^{(r)}(t)$, and the former may in fact not really be considered as localized with respect to the latter. With these provisos in mind, we can proceed to write the Markovian version of Eqs. (5), (10), (12) and (13):

$$\underline{K}(t) = (\underline{\Omega} + \underline{f}) \delta(t) , \qquad (16)$$

$$\underline{P}(t) = \underline{W} \cdot \underline{P}(t) , \qquad (17)$$

$$\underline{J}(s) \cdot \underline{P}(s) = \underline{U} , \qquad (18)$$

where

$$\underline{\mathbf{f}} = \underline{\mathbf{k}} \ \tau \ , \tag{19}$$

$$\underline{W} = \underline{\Omega} + \underline{f} , \qquad (20)$$

$$J(s) = (\Omega + f - s\Delta) , \qquad (21)$$

$$\underline{\mathbf{U}} = -\underline{\mathbf{P}}(0) , \qquad (22)$$

and τ represents the actual extent of the laser signal or a variable time parameter. Equation (17) is the well-known Pauli master equation (PME). 1,6

To summarize the formulation, Eq. (10) is the exact GME with a convolution type kernel which makes solutions difficult for experimental times. If the kernel can be approximated as the sum of a very sharply peaked function due to the phonons plus a constant due to the laser (the isomnesic approximation), we get the simplified GME, Eq. (11), which is still not Markovian but has a "constant memory" (isomnesic-) term. The resulting second-order differential equation, Eq. (12), can be solved analytically for arbitrarily long times. If, on the other hand, memory effects are assumed to be negligible, i.e., with a kernel highly localized in time, Eq. (3), we get the Markovian limit, namely the PME, Eq. (17), which is a first-order differential equation and can also be solved analytically for arbitrarily long times. The nature of the solutions depends, of course, on the time paramter τ in Eq. (19).

III. Results of the Exact, Isomnesic and Markovian Approximations

For a linear-chain model of the solid, the exact kernel function due to phonons alone, $\underline{K}^{(p)}$, involves an expansion over the number of phonons n and the number of lattice atoms ℓ . For the specific system chosen, the effective surface potential generates five bound states; we have chosen $|\omega_{01}| = \omega_{D}$ and $|\omega_{13}| = \omega_{L} [\omega_{SS}] = (\ell_{S} - \ell_{S})/\hbar$; see Eq. (2)]. The phonon kernels, e.g., $K_{01}^{(p)}(t)$ in Fig. 1, fall off quite rapidly in time and arise almost entirely from the (n=1, ℓ =1) term.

At issue is the validity of the isomnesic and Markovian approximations. We can examine two aspects of the results, viz. the details of the early transient behavior, and the long-term steady state. For the Markovian case, we can further examine the effects of varying τ in Eq. (19). The transient behavior can be compared with exact numerical solutions of Eq. (10), but the steady-state results of the MA and the IA can only be judged by extrapolation.

While the probability profiles $\underline{P}(t)$ provide sufficient comparison, the physical contents of our results are better displayed by the average adbond energy given by

$$\boldsymbol{\xi}(t) = \sum_{S} P_{S}(t) \boldsymbol{\xi}_{S} , \qquad (23)$$

where $\mathbf{6}_{\mathrm{S}}$ is the energy eigenvalue corresponding to the level 'S> of the effective adbond potential. This provides a simple measure of the chemical direction of the adbond and a well-defined connection between this exact theory and phenomenological models of such processes.

The results obtained by solving Eqs. (10), (12) and (17) for a variety of situations of physical interest are very consistent, and we present a typical set of curves in Fig. 2 for early times, $t \le 5$ ps. The exact results are rich in detail and, to a large degree, follow the variations in $\underline{K}(t)$. We shall not dwell on the physical contents except to mention the conspicuous absence of the simple exponential approach to equilibrium postulated in relaxation time theories. The results of the IA, while exhibiting the expected loss of the fine detail, are seen to chart out the <u>average</u> behavior of $\underline{P}(t)$ with great accuracy. Thus, for example, the crossing point of $\underline{P}(t)$ and $\underline{P}(t)$ is reproduced at t = 1.7 ps as compared to the exact crossing point at 2.2 ps, and the difference $\underline{P}(t) - \underline{P}(t)$ is seen to follow the exact difference with a similar slight

temporal retardation. The gross oscillations of P(t) are also reproduced faithfully. Consequently, we feel confident in our prediction that the steadystate results of the IA will conform to the exact results very accurately. We wish to emphasize the significance of this. The IA makes possible the complete solution of a GME for arbitrarily long times, when the solution of the exact GME is essentially impossible. The solution of the GME in the IA is no more difficult than that of the PME obtained by invoking the MA which, however, gives results which differ radically from the exact results in the transient region for a wide range of values of τ . Figure 3 illustrates the variations of $P_S(t)$ with τ in the MA (10⁻⁵ ps $\leq \tau \leq 10^5$ ps). The probability profiles are seen to be insensitive to increases in τ beyond ~ 10 ps, which corresponds to almost instantaneous saturation. The apparent insensitivity of $\underline{P}(t)$ for $\tau \le 10^{-2}$ ps seen in Fig. 3 is, of course, misleading, since in this region the $P_S(t)$ vary with time too slowly for the change to be evident in the 20 ps time range of the plot. Drawn for 2 ns in Fig. 4 [we present only $P_3(t)$], the differences become more pronounced for $\tau < 10^{-2}$ ps, and the strong dependence of the apparent "equilibration time" on τ emerges clearly. We see no unambiguous way of choosing an appropriate value for τ . For systems which are known or expected to equilibrate very quickly, one could make an ad hoc semiempirical choice of τ to solve a PME for the steady state. However, if one is interested in the details of the short-time behavior of the system, one must solve the GME using the IA.

For comparison of the MA with the IA we have chosen τ = 1 ps. The resulting profiles for the MA are shown in Fig. 5, along with our IA results for 20 ps. The complete absence of oscillatory behavior representing beats of the system and of population crossings, and the presence of predominantly exponential variation of P(t) representative of a "relaxation time" exhibited by the MA

results of Fig. 5 are not necessarily general features of the solutions of a PME. Since the matrices M and J are, in general, asymmetric, both the GME and the PME can generate oscillatory solutions P(t), contradicting earlier contentions. However, the total lack of resemblance between the early PME results and the exact ones for the present case is alarming and raises urgent and serious questions about the validity of the Markovian approximation, even for a rough qualitatiave estimate of the early transient behavior of many-body systems with a nonrandom force. At best, these results suggest the need for great caution in using the MA. In retrospect this is not surprising, because the representation of a time-independent cw laser beam by an ultrashort pulse is tenuous, whereas that of the very-short-range (in time) phonon correlation by a delta function is quite reasonable.

The results for ξ (t), shown in Fig. 6 for the exact GME and the IA and in Fig. 7 for the MA and the IA further support these contentions. The IA generates an energy profile which, except for a slight temporal retardation, is a low-resolution representation of the exact result. The significant increase in the bond energy at the expense of both the laser and the solid is clearly evident in the IA results of Figs. 2 and 6. The results of the MA are qualitatively different from the exact and IA results, and describe a monotonic approach to the steady state. The exact and IA results show actual periodic energy transfer out of the adbond followed by successive build up due to overall energy inflow. The apparent correspondence seen in Fig. 7 between the magnitude of ξ (t) in the MA and the "base line" about which the results of the exact GME and the IA oscillate is entirely due to our choice of τ = 1 ps. That no such correspondence can be expected in general is evident from Fig. 8 showing the variations of ξ (t) with τ . The steady-state (t+ ∞) values of P(t) and ξ (t) in

the MA have been found to be the same as those obtained with the IA for all cases considered so far (when the values of τ chosen lead to steady states in the time ranges considered).

IV. Conclusion

Our results for the time evolution of a dynamical many-body system subject to a variety of forces point out the inadequacies of the Markovian approximation when the resulting memory kernel is nonlocal in time. As an alternative, we present the isomnesic approximation which is characterized by a constant memory; this eliminates the non-Markovian bottleneck associated with the convolution-type memory kernel in the Volterra-type integrodifferential equation resulting from the generalized master equation. Closed solutions of the latter are in excellent agreement with the exact results, in contrast to those of the Markovian approximation.

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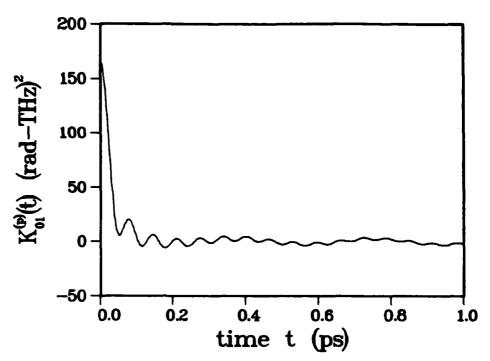
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Figure Captions

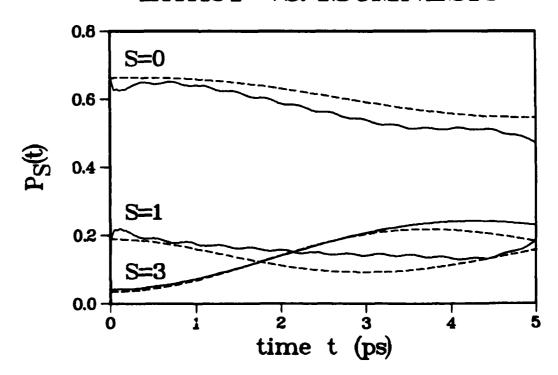
- Fig. 1. The phonon part $K_{01}^{(P)}(t)$ of the memory kernel.
- Fig. 2. Probability profiles $P_S(t)$ for levels S=0, 1 and 3 of the adbond. Solid lines: Exact numerical solutions of the GME; broken lines: closed-form solutions of the GME with the IA.
- Fig. 3. $P_S(t)$ for the system of Fig. 2 with the MA for a ten-decade range of τ . (A)- $P_O(t)$; (B)- $P_1(t)$; (C)- $P_3(t)$.
- Fig. 4. $P_3(t)$ with the MA for 2 ns.
- Fig. 5. Comparison of $P_{S}(t)$ with the IA (solid lines) and the MA ($\tau\text{=}1$ ps; broken lines) for S=0, 1 and 3
- Fig. 6. Average adbond energy &(t) obtained via the numerical solution of the exact GME (solid line) and closed-form solution with the IA (broken line).
- Fig. 7. $\mathcal{E}(t)$ with the IA (solid line) and the MA ($\tau=1$ ps; broken line).
- Fig. 8. Variation of G(t) with τ in the MA.

MEMORY KERNEL

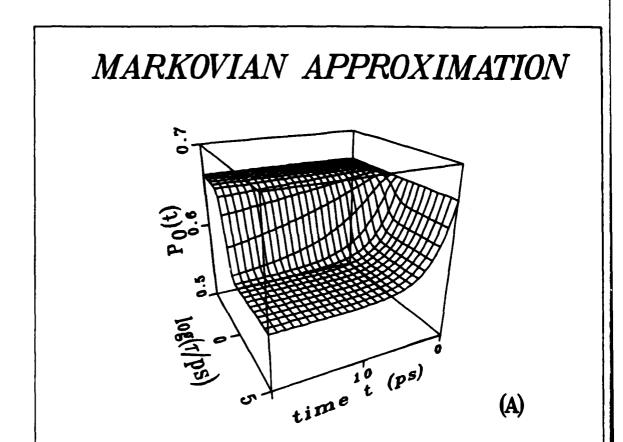


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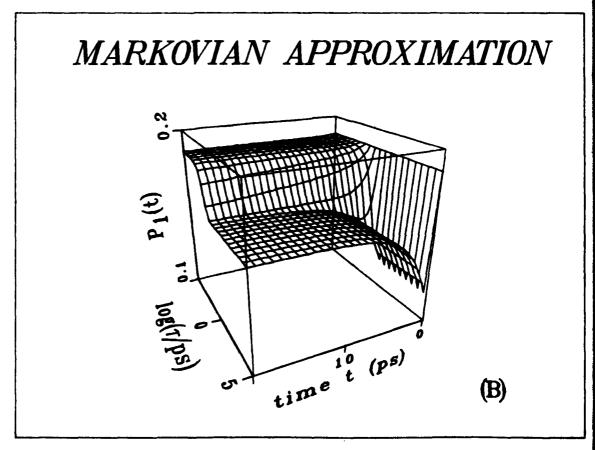
EXACT vs. ISOMNESIC



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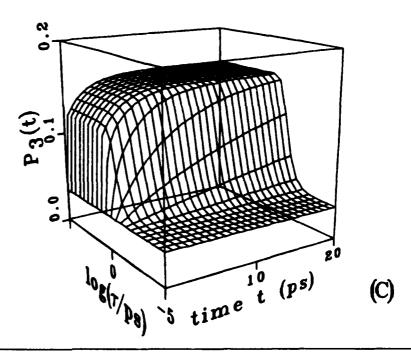


Beri/Greerge Fig 3(A)



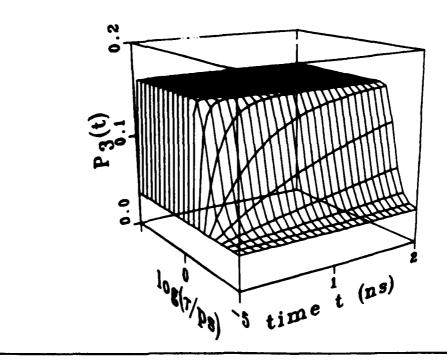
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MARKOVIAN APPROXIMATION



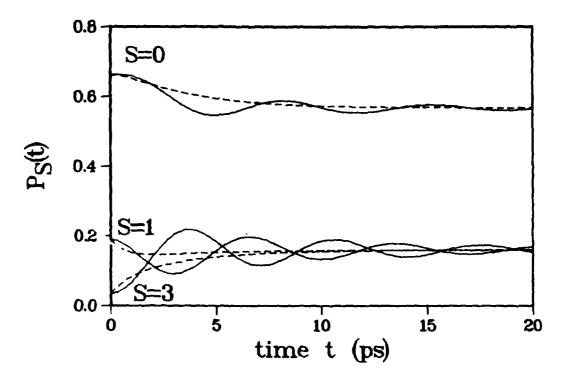
Beri/George Fig 3 (c)

MARKOVIAN APPROXIMATION



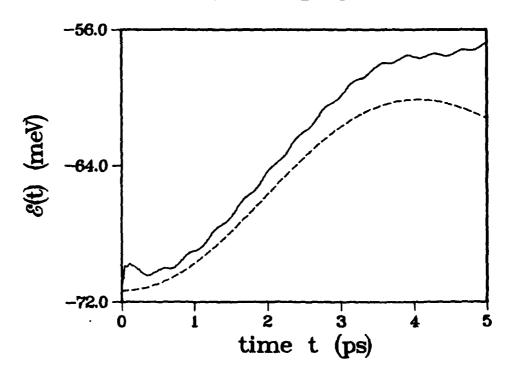
Ber/Gerric Fig4

ISOMNESIC vs. MARKOVIAN



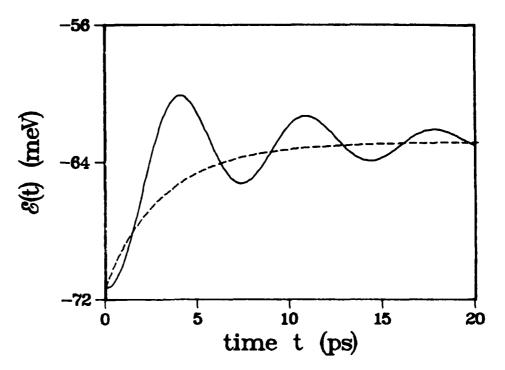
BerilGeorge Fig 5

EXACT vs. ISOMNESIC

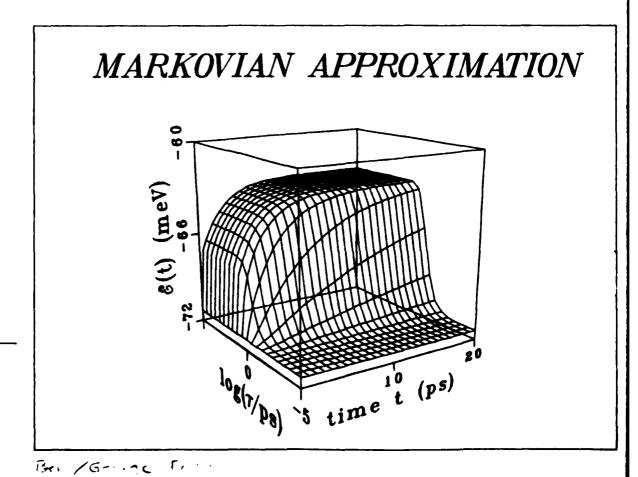


Berilacine Fige

ISOMNESIC vs. MARKOVIAN



Ber/George Fig 7



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